



FEDERAL PUBLIC SERVICE COMMISSION
COMPETITIVE EXAMINATION-2024 FOR RECRUITMENT
TO POSTS IN BS-17 UNDER THE FEDERAL GOVERNMENT
APPLIED MATHEMATICS

Roll Number

TIME ALLOWED: THREE HOURS

MAXIMUM MARKS = 100

- NOTE: (i)** Attempt only **FIVE** questions in all. **ALL** questions carry **EQUAL** marks.
(ii) All the parts (if any) of each Question must be attempted at one place instead of at different places.
(iii) Write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.
(iv) No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
(v) Extra attempt of any question or any part of the attempted question will not be considered.
(vi) **Use of Calculator is allowed.**

Q. No. 1 (a) Expand a fourier series of $f(x) = x^2, 1 < x < 2$ (10)

(b) Find equation of integral surface of the differential equation $2y(z-3)p + (2x-z)(10)$
which passes through the circle $x^2 + y^2 = 2x, z = 0$.

Q. No. 2 (a) Solve the higher order differential equation $y'''' + y'' = 3x^2 + 4\sin x - 2\cos x$ (10)

(b) Solve the initial value problem $y'' - 8y' + 15y = 9xe^{2x}, y(0) = 5, y'(0) = 10$ (10)

Q. No. 3 (a) Solve the equation $4u_{xx} + 5u_{xy} + u_{yy} + u_x + u_y = 2$, also find its canonical form. (10)

(b) Prove that $\int_{-1}^1 x^n P_n(x) dx = \frac{2^{n+1} (n!)^2}{(2n+1)!}$, where $P_n(x) = \frac{1}{2^n n!} \frac{d^n}{dx^n} (x^2 - 1)^n$ is (10)
Legendre polynomial of degree n .

Q. No. 4 (a) Verify the divergence theorem for $A = 4xi - 2y^2j + z^2k$ taken over the region (10)
bounded by $x^2 + y^2 = 4, z = 0$ and $z = 3$.

(b) State and prove Stoke's theorem. (10)

Q. No. 5 (a) Using the modified Euler's method, obtain the solution of the differential equation (10)

$$\frac{dy}{dt} = t + \sqrt{y} = f(t, y)$$

with initial condition $y_0 = 1$ at $t_0 = 0$ for the range $0 \leq t \leq 0.6$ in step of 0.2 .

(b) Find the real roots of equation $4x + \cos x + 2 = 0$ by using Newton Raphson (10)
method, correct to four decimal places.

Q. No. 6 (a) Solve the system of linear equations by Gauss-Seidel iterative method and perform (10)
the first three iterations of

$$\begin{aligned} 20x + y - 2z &= 17 \\ 3x + 20y - z &= -18 \\ 2x - 3y + 20z &= 25 \end{aligned}$$

APPLIED MATHEMATICS

- (b) Solve the following Van der Pol's equation $y'' - (0.1)(1 - y^2)y' + y = 0$, (10)

using fourth order Runge-Kutta method for $x = 0.2$, with the initial values

$$y(0) = 1, \quad y'(0) = 0.$$

- Q. No. 7 (a) Find the law of force for a particle moving in an orbit, $r = \frac{l}{1 - e \cos \theta}$, where l is (10)

semi latus rectum and e is eccentricity.

- (b) Prove that the speed required to project a particle from a height h to fall a (10)

horizontal distance a from the point of projection is at least $\sqrt{g(\sqrt{a^2 + h^2} - h)}$.

- Q. No. 8 (a) Find the radial and transvers components of velocity moving along a curve $a x^2 + b$ (10)

at any time t if the polar angle $\theta = c t^2$.

- (b) Find the centroid of the surface formed by the revolution of the cardioide (10)

$r = a(1 + \cos \theta)$ about the initial line.
